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# Modelling country and group levels corporate default dependence: Evidence from the Euro area

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#### Abstract

This paper employs a mixed e ects Cox model to estimate the failure dependence caused by rms' exposure to unobserved factors at both country and group level. We use a quarterly panel data set of 1,422 public listed rms across the Euro area over the period 1994Q1-2014Q4. The empirical analysis delivers three main results. First, when countries are grouped together, with economic and nancial similar conditions, failure clustering tend to be larger, as rms are subject to an extra risk due to the impact of unobserved factors at the group level. Second, there is signi cant evidence of failure dependence caused by rms' exposure to country level unobserved factors. Third, models that do not account for the distance to default probability tend to perform poorly as compared with their counterparts.

Keywords: Hazard rates; mixed e ects model; country and group level dependence; Eurozone

JEL Classi cation: G33, C51, C41.

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# 1 Introduction

The nancial crisis and the sovereign debt crisis hit the Euro area signi cantly. Not only the PIIGS contries, but also Belgium and France were a ected (Metiu, 2012; Arghyrou and Kontonikas, 2012; Ludwig, 2014), even though to a lesser extent.<sup>1</sup> As a result, banks were more conservative with their lending activities, and a large reduction in loan supply was observed, with an impact on investment activities, job creation, and sale growth (Acharya et al., 2016). Since then, business entities within the Euro have struggled to survive, and the hazard rates of these businesses have been severely a ected, due to their exposure to risk factors at country and group level.

Das et al. (2007) observed excess default correlation induced by unobserved factors (or frailty factors), and showed that models based on the assumption that corporate defaults are conditionally independent after adjusting for observable factors tend to underestimate default clustering. Against this background, several studies have considered failure dependence induced by unobserved risk factors at country or industry levels using frailty factors (see e.g. Du e et al., 2009; Chava et al., 2011; Koopman et al., 2011, 2012; Qi et al., 2014) so to yield more accurate estimates of hazard rates.

In this paper, we estimate the failure dependence of 1,422 public listed rms in 11 Eurozone countries over the period 1994Q1-2014Q4. The analysis is conducted at country and group level. As for the group level, we consider PIIGS and non-PIIGS countries, since the strong linkage between economic conditions and rm performance (see e.g Bhattacharjee et al., 2009; Bon m, 2009; Chen, 2010; Tang and Yan, 2010; Jacobson et al., 2013). In addition, we consider three extra groups that are formed by including: only Belgium in the PIIGS (PIIGSB); only France in the PIIGS (PIIGSF); both Belgium and France in the PIIGS (PIIGSBF) (see also Giordano et al., 2013). This allows us to establish to what extent the crisis in the Euro area

and Janssen, 2008; Wienke, 2011) within a multivariate framework of mixed e ects Cox model (see Ripatti and Palmgren, 2000; Therneau and Grambsch, 2000; Therneau et al., 2003). A cluster level-speci c random e ect, which is assumed to follow a Gaussian distribution, is considered for country and group level clustering, and rms in each country are exposed to country (internal) and group level (external) risk (unobserved) factors. We also consider a non-nested frailty model, which accounts only for country level (internal) unobserved factors ( rms are not exposed to any potential external risk factors). This model is considered for comparison purposes. It is expected that the estimates of the nested frailty model will likely be more accurate than those by the non-nested frailty model, due to the fact that the latter ignores the potential impact of externals factors. This may suggest that the total risk exposure of a rm is not only limited to country level factors, but also to bloc level factors. Therefore,

the Euro area. Third, models that account for the distance to default probability covariate

### 2.1 Non-nested frailty models

Let  $T_{ij}$  and  $_{ij}$  respectively be the event time and event indicator (censoring indicator) of rm *i* listed in country *j* among *q* countries. The indicator  $_{ij}$  takes the value 1 if  $T_{ij}$  is a failure time and 0 otherwise. Suppose that the data set of rm *i* follows a shared frailty model. The hazard rate of the rm is de ned as follows (see Ripatti and Palmgren, 2000; Therneau et al., 2003; Duchateau and Janssen, 2008, among others):

$$_{ij}(t) = _{0}(t)u_{j}exp(X_{ij}(t));$$
(1)

where  $_{ij}(t)$  is the hazard rate of rm *i* listed in country *j*, and  $X_{ij}(t)$  and are vectors of

(2) is normally distributed on the log-scale, and the parameters and *w* are estimated by maximizing the penalised partial likelihood (PPL):

$$PPL = PL(; w; data) \quad g(w; );$$
(3)

where *PL* is de ned as the log of the classical Cox partial likelihood conditioned on the data set:

$$PL(;w) = \sum_{i=1}^{N} \sum_{i=1}^{Z} \frac{1}{i} h_{i}(t)(exp(X_{i} + Z_{i}w)) \log \sum_{k}^{X} Y_{k}(t)(exp(X_{k} + Z_{k}w)) dN_{i}(t); (4)$$

and the penalty term is de ned by

$$g(w; ) = \frac{1}{2} \sum_{j=1}^{N} w_j^2;$$
 (5)

where is the variance of the log-frailty or random e ect.<sup>3</sup> For a given value of the variance estimate , we use the expansion and approximation of Ripatti and Palmgren (2000) to derive a modi ed likelihood de ned as:

$$I_{m}(;) = \frac{1}{2}\log(jDj) + \log \sum_{\substack{w \in D \\ v \in D}} \frac{1}{2} \log(jDj) + \log \sum_{\substack{w \in D \\ v \in D}} \frac{1}{2} \log w^{\theta} D^{-1=2} w + \log(jDj) + \log(jH_{22}(;w)); \quad (6)$$

where D = I is a diagonal matrix and I is an identity matrix of order q = q; q is the number of countries in the sample, and  $g(w; ) = w^{\rho}D^{-1}()w$ . The term w = w(; ) solves the following equation

$$\sum_{j=1}^{N} \sum_{i=1}^{Z_{j}} (Z_{ij} - Z_{j}(t)) dN_{i}(t) \quad D^{-1}(\cdot) W = 0$$
(7)

<sup>&</sup>lt;sup>3</sup>For details on penalised partial likelihood of a shared frailty model, see Ripatti and Palmgren (2000) and Therneau et al. (2003).

The coe cients of equation (9) can still be estimated without knowing the shape of  $_0$ . The random e ects distribution *G* is a multivariate Gaussian distribution with zero mean and variance matrix  $\stackrel{P}{}$ , which is a function of a vector of the parameters . Following Therneau and Grambsch (2000) and Therneau et al. (2003), we de ne the log penalised partial likelihood function as follows:

$$PPL(;b;) = I(;b) \quad g(b;);$$
(10)

where the penalty function  $g(b; ) = b^{p-1}()b=2$ . The term I(; b) is called the partial likelihood (PL) (see Therneau, 2015) for any given value of and b, and is defined as:

$$I(;b) = \frac{\chi_{ij} Z_{i} h}{\sum_{k=1}^{N} Y_{k}(t) k(t)} X_{k}(t) Iog X_{j}(t) idN_{k}(t);$$
(11)

where  $_{k}(t) = X_{k}(t) + Z_{k}(t)b$  is the linear score for rm k at time t,  $X_{k}(t)$  and  $Z_{k}(t)$  are the  $k^{th}$  rows of the covariate matrices X and Z, respectively. In other words, the above row matrices are the data set for rm k in country j. The term  $Y_{k}(t)$  describes the surviving rms (or rms still at risk of default), which takes value 1 when rm k is active at time t, and 0 otherwise. Equation (10) can then be re-written as:<sup>4</sup>

$$PPL(;b;) = \frac{\chi_{ij} Z_{1} h}{\sum_{k=1}^{N} Y_{k}(t) k(t)} X_{k}(t) \log \frac{Y_{j}(t) j(t)}{j} \frac{dN_{k}(t)}{dN_{k}(t)} \frac{b^{0}}{2} \frac{P_{1}()b}{2}.$$
 (12)

The estimates of and b,  $\hat{b}$ , are obtained by solving the following score equations (see Therneau et al., 2003):

$$\frac{@PPL}{@b_j} = \sum_{\substack{i=1 \\ j=1 \\ 0}}^{N^1 \ Z_j} (Z_{ij} \ Z_j(t)) dN_i(t) \quad \frac{@g(b_i)}{@b_j};$$
(13)

<sup>&</sup>lt;sup>4</sup>For detailed treatment, refer to Therneau et al. (2003).

$$Z_{j}(t) = Z_{j}(j;b;t) = \frac{P_{kj}Z_{kj}Y_{k}[X_{k} + Z_{k}b]}{Y_{k}[X_{k} + Z_{k}b]}$$
(14)

We also obtain the integrated partial likelihood (IPL) by integrating out the random e ects as obtained below (Therneau, 2015):

$$IPL = \frac{1}{(2)^{q=2}j} \left( \begin{array}{c} 1 \\ 1 \\ 1 \end{array} \right)^{2} PPL(; b^{0} \\ 1 \\ 1 \end{array} \right) exp \qquad b^{0} \\ b^{0} \\ 1 \\ b = 2 \\ db; \qquad (15)$$

where q is the number of random e ects. We estimate the parameters using the coxme'' package in R by (Therneau, 2015).

#### 2.3 Data

Our data are drawn from DataStream and Worldscope for public listed rms in 11 member states of the Eurozone for the period 1994Q1-2014Q4. The sample is comprised of 1,422 rms: 905 active rms, 398 failed rms and 119 acquired or merged rms, and this translates into 71,680 quarterly rm observations. The countries are Austria, Belgium, Finland, France, Germany, Greece, Ireland, Italy, Netherlands, Portugal, and Spain. The choice of these countries is based on data availability.<sup>5</sup> Table 1 presents rms' status at country level across the 11 selected members of the Eurozone.

The de nition of rm failure may di er across all the member states of the Euro area. For the sake of uniformity, we follow Altman and Narayanan (1997), who provide a de nition of failure: (i) ling by a company; (ii) bond default; (iii) bank loan default; (iv) delisting of a company; (v) government intervention via special nancing; and (vi) liquidation.<sup>6</sup> We select failed, and acquired or merged rms from the DataStream \DEAD" category for each country in conjunction with other sources (e.g. Bloomberg bankruptcy segment). For instance, DataStream items \DEADGR", \DEADBD" and \DEADFR" are the categories for dead

<sup>&</sup>lt;sup>5</sup>These countries may have some accounting information disclosure di erences, but Worldscope adjusts the variables for these di erences.

<sup>&</sup>lt;sup>6</sup>For delisting of a company, we cross check the reasons for delisting at other sources. These reasons include mergers, acquisitions and some of the reasons already stated.

Table 1: Active, failed and merged or acquired rms within the Eurozone

since the rm is censored as a result of a non-failure event.<sup>7</sup>

We employ some widely used covariates in the empirical literature of corporate failure, given their explanatory power (see Shumway, 2001; Du e et al., 2007, 2009; Duan et al., 2012; Qi et al., 2014, among others). First, we use the 3 month T-bill rate, which is a measure of short-term interest rates. Second, we consider the one year trailing stock return, which is a good predictor of rm failure (see Shumway, 2001), and is constructed by cumulating monthly stock returns. Third, we use the one year trailing market return, which is a measure of the overall market performance, and is constructed by cumulating monthly market returns. Fourth, the distance to default probability is used as a probabilistic measure of volatility adjusted leverage. In constructing this measure, we follow Bharath and Shumway (2008): rms with higher probabilities are close to default, whilst rms with lower probabilities are

far from default. Lastly, we consider the age of a rm to test whether older rms are less

the mean than the latter. Additionally, the natural log of rm age is bounded by (0.000, 2.996) since the rm age falls within the interval [1, 21]. The 3 month T-bill rate ranges from 1.123% to 12.144%.

# 3 Empirical analysis

This section presents the empirical results obtained using non-nested and nested frailty models. More speci cally, we rst estimate the parameters of the non-nested frailty model, which serves as benchmark model. Then the parameters of the nested frailty model are estimated, and its performance is compared to that of the non-nested model. Lastly, we compute the total riskiness of rms in order to evaluate how rms are a ected by country and group level unobserved factors.

In our analysis, we consider PIIGS countries against non-PIIGS ones along with three extra groups that are formed by including: only Belgium in the PIIGS (PIIGSB); only France in the PIIGS (PIIGSF); and both Belgium and France (PIIGSBF). In other words, we extract the country and group level frailty factors that a ect listed rms for following pair of groups: (i) PIIGS versus non-PIIGS; (ii) PIIGSB versus non-PIIGSB; (iii) PIIGSF versus non-PIIGSF; and (iv) PIIGSBF versus non-PIIGSBF.

In the regression analysis, we employ distance to default probability, one year trailing stock return, one year trailing market return, In(age), and 3 month T-bill rate as covariates. Table 3 reports the estimates for non-nested frailty models. For model 1, the hazard rate

and Shumway, 2008). This implies that, for an appropriate default model speci cation, the distance to default probability should be augmented with suitable covariates. Model 3, which we consider to perform a con rmatory test on the distance to default probability, also shows the insigni cance of the 3 month T-bill rate, while the other covariates are signi cant.

To nd the best model in terms of goodness of t across all the speci cations, we use both the pseudo-deviance and the information criteria measures. For the former criterion, we have:

$$Pseudo-deviance = 2loglik_{A} + 2loglik_{B};$$
(16)

where  $2loglik_A$  and  $2loglik_B$  are the deviance statistics for generic models A and B, respectively. The statistic in (16) says how model A performs worse than the supposed best model B, and it can be used in case of nested models. The statistic follows a chi-square distribution (<sup>2</sup>), with the degrees of freedom being the di erence between the number of parameters in model A and that in model B.

As for the information criteria, we consider the Akaike information criterion (AIC), the corrected Akaike information criterion (AICC), and the Bayesian information criterion (BIC):

$$AIC = 2logL + 2k; \tag{17}$$

$$AICC = AIC + \frac{2k(k+1)}{n-k-1}$$
 (18)

$$BIC = 2logL + klogn; \tag{19}$$

where 2*LogL* is the partial likelihood, which is obtained by using the rank of events (Singer and Willett, 2003), *k* and *n* denote the number of parameters and events, respectively (see Raftery, 1995). As a rule of thumb, the lower the values of these information criteria, the better the t. The information criteria are suitable for both non-nested and nested models. Since model 2 nests model 1, and model 4 nests model 2, we use the pseudo-deviance to compare the performance of these models. In case of models 1 and 2 (the latter nests the former), the pseudo-deviance statistic is equal to 31:480(5173:580 5142:100), with 3 degrees of freedom. Since the value of the statistic is greater than the critical value,  $\frac{2}{0.01(3)} = 16:266$ , the null hypothesis that the coe cients of stock return, market return and In(age) are all equal zero can be rejected. This implies an improvement of the t due to the inclusion of these covariates, which makes model 2 the best candidate. Similarly, the values of this statistic for models 1 and 4 is 31:876, which is larger than the critical value  $\frac{2}{0.01(4)} = 18:467$ . Therefore, model 4 ts the data better than Model 1. Instead, a di erent result is found for models 2 and 4. Here, the value of the pseudo-deviance statistic, 0:396, is smaller than the critical value,  $\frac{2}{0.01(1)} = 10.828$ . Therefore, there is no improvement in terms of t if one adds 3 month T-bill rate to model 4. Likewise, for models 3 and 4, the test statistic is 63.296 with  $\frac{2}{0.01(1)} = \frac{10}{0} \frac{10}{32}$ 

Dependent variable: Time to event						
	Model 1	Model 2	Model 3	Model 4		
Distance to default prob.	1.221	0.929		0.925		
	(0.231)	(0.255)		(0.255)		
Stock return		-0.298	-0.490	-0.291		
		(0.143)	(0.140)	(0.144)		
Market return		-0.559	-0.482	-0.501		
		(0.276)	(0.290)	(0.290)		
In(age)		-0.384	-0.375	-0.386		
		(0.082)	(0.081)	(0.082)		
3 month T-bill rate			-3.814	-3.125		
			(4.960)	(4.968)		
LogLik.(Fitted)	-2572.592	-2557.045	-2588.069	-2556.648		
LogLik.(Integrated)	-2586.790	-2571.050	-2602.738	-2570.852		
Integrated LR test	80.140	111.620	103.110	112.020		
	[0.000]	[0.000]	[0.000]	[0.000]		
Penalized LR test	108.540	139.630	132.450	140.430		
	[0.000]	[0.000]	[0.000]	[0.000]		
Pseudo-deviance	5173.580	5142.100	5205.476	5141.704		
AIC	5175.580	5150.100	5213.476	5151.704		
AICC	5175.601	5150.315	5213.691	5152.028		
BIC	5175.861	5151.224	5214.600	5153.109		
Dependence	0.185	0.179	0.203	0.186		

Notes: The efron approximation is used to control for ties in the event times of rms. Standard errors and p-values are in round and square brackets, respectively. , denote signi cance at the 1%, 5%, and 10% level, respectively. LogLik.(Fitted) and LogLik.(Integrated) are the tted and integrated likelihoods due to unobserved factors, respectively. The terms Integrated LR and Penalized LR denote the unobserved factors-adjusted integrated and penalized likelihood ratio tests, respectively. The pseudo-deviance is used to compare the overall model t of nested models, while the Akaike information criterion (AIC), corrected Akaike information criterion (AICC), and Bayesian information criterion (BIC) measures are used to compare either nested or non-nested models.

rms that usually exhibit averagely higher distance to default probability are more prone to experience failure within the Eurozone. Second, a rise in stock return and market return increases the expected time to default. This outcome seems to suggest that rms listed within the Euro area with a consistent increase in their returns are less likely to move towards a failure point, and performing markets tend to enhance the survival rate of such rms, as compared to those of averagely decreasing stock returns. Third, the signi cance of age in our models reveals that older rms in Euro area are less likely to fail than the younger ones. This may be due to the liability of newness (see e.g Baum, 1996; Aldrich and Ruef, 2006; Wiklund et al., 2010), as older rms may have more business contacts, better understanding of the dynamics of the business environment and more robust organisational structure. Further, older rms

as our benchmark model.

The empirical results are illustrated in Tables 4 and 5. In all models, almost all the regressors are signing cant with the expected signs. For example, in the  $D_{PG}$  model, the coeccient of distance to default probability is positive and signi cant, and those of the stock return, market return, and In(age) are negative and signi cant. While these results do not di er from those in Table 3, measures of dependence have improved considerably, regardless of the speci cation of the model. This implies that when determining risk rates of listed rms in an economic bloc during unfavourable market and economic conditions, it is more appropriate to group countries according to similar macroeconomic structures. Failure to do so may lead to underestimation of risk rates, since non-nested models are based on the hypothesis that countries are independent to each other. As such, the economic and nancial activities between member states have no signi cant impact on rms, and the macroeconomic conditions in one or more countries may be not transmitted to another. Therefore, the risk level of rms is restricted to only country level, and the potential group level exposure is ignored in the estimation parameters. On the contrary, nested models assume dependence among member states through the interaction of countries. Therefore, using these models more accurate estimates of the risk level can be gained.

We complete our analysis with an investigation of the impact of rms' membership to the diverse groups of the Euro area on riskiness. In Table 6, we report results related to the risk scores and the level of riskiness of rms within countries, and PIIGS and non PIIGS group of countries. In the event of failure clustering, the country (group) score shows how rms are likely to fail either faster or slower. As such, we use value 1 (expected value of frailty) as a threshold value for gauging riskiness. A risk-score large than 1 implies more riskiness, while a score lower than 1 is considered less riskiness. Examples of more risky countries are Austria, Finland, Greece, Ireland, Netherlands and Portugal, while the less risky countries are Belgium, France, Germany, Italy and Spain. For instance, the risk scores for Portugal and Belgium are 1.231 and 0.984 respectively, values that are shared by rms in these countries. The country

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Dependent variable: Time to event						
	PII	GSB	PIIC	GSF		
	$D_B$	S <sub>B</sub>	$D_F$	$S_F$		
Distance to default prob	1.331	0.847	1.349	0.876		
	(0.277)	(0.258)	(0.277)	(0.258)		
Stock return	-0.272	-0.320	-0.262	-0.317		
	(0.145)	(0.147)	(0.145)	(0.149)		
Market return	-0.712	-0.732	-0.757	-0.752		
	(0.318)	(0.311)	(0.321)	(0.311)		
In(age)	-0.369	-0.356	-0.378	-0.391		
	(0.084)	(0.096)	(0.084)	(0.097)		
LogLik.(Fitted)	-1839.700	-2487.728	-1788.692	-2451.328		
LogLik.(Integrated)	-2560.389	-2592.065	-2563.549	-2592.324		
Integrated LR test	132.940	69.590	126.620	69.070		
-	[0.000]	[0.000]	[0.000]	[0.000]		
Penalized LR test	1574.320	278.260	1676.340	351.060		
	[0.000]	[0.000]	[0.000]	[0.000]		
Psuedo-Deviance	5120.778	5184.130	5127.098	5184.648		
AIC	5128.778	5192.130	5135.098	5192.648		
AICC	5128.993	5192.345	5135.313	5192.863		
BIC	5129.902	5193.254	5136.222	5193.772		
Dependence	1.929	0.288	2.094	0.398		

# Table 5: Nested frailty models: PUGSB and PUGSE groups

Notes: Standard errors and p-values are in round and square brackets, respectively. D<sub>B</sub> and S<sub>B</sub> indicate the models for PIIGSB with similar trends in terms of the distance to default and stock returns respectively, whereas  $D_F$  and  $S_F$  are the models for the PIIGSF. , denote signi cance at the 1%, 5%, and 10% level, respectively. For further details, see Table 3.

	County level		<i>D<sub>PG</sub></i>			S		
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
	Country	Country	Group	Group	Total	Group	Group	Total
PHGS	Score	Riskiness	Score	Riskiness	Riskiness	Score	Riskiness	Riskiness
Portugal	1.231	0.231	1.092	0.092	0.323	1.134	0.134	0.365
	1.423	0.423	1.092	0.092	0.010	1.134	0.134	0.007
Italy	0.729	-0.271	1.092	0.092	-0.179	1.134	0.134	-0.137
Greece	1.449	0.449	1.092	0.092	0.541	1.134	0.134	0.583
Spain	0.777	-0.223	1.092	0.092	-0.131	1.134	0.134	-0.089
non-PIIGS								
Austria	1.793	0.793	0.915	-0.085	0.708	0.882	-0.118	0.675
Belgium	0.984	-0.016	0.915	-0.085	-0.101	0.882	-0.118	-0.134
Finland	1.044	0.044	0.915	-0.085	-0.041	0.882	-0.118	-0.074
France	0.583	-0.417	0.915	-0.085	-0.502	0.882	-0.118	-0.535
Germany	0.536	-0.464	0.915	-0.085	-0.549	0.882	-0.118	-0.582
Netherlands	1.209	0.209	0.915	-0.085	0.124	0.882	-0.118	0.091

Table 6: Scores and riskiness for nested frailty models: PIIGS versus non-PIIGS

Notes:  $D_{PG}$  (columns 3 to 5) and  $S_{PG}$  (columns 6 through 8) refer to PIIGS countries which have similar behaviour of distance to default probability and stock return, respectively. Figures in columns (1) and (2) indicate country-level scores and riskiness, respectively. Figures in column (2) are obtained by subtracting value 1 (expected value of the unobserved factors) from numbers in column (1). Figures in columns (4) and (7) are obtained by subtracting value 1 from gures in columns (3) and (6). Total riskiness for  $D_{PG}$  and  $S_{PG}$ are constructed by adding gures in columns (2) to those in column (4), and numbers in column (2) to those in column (7), respectively. followed by Ireland and Portugal, while France has the lowest risk level. For the non-PIIGSBF

and PIIGSF groups. The following results are obtained. The risk score falls within the range (1.121, 1.153) and (1.000, 1.003) for PIIGSB and PIIGSF, respectively. Thus, the group riskiness, when Belgium is regarded as a member of the PIIGS, falls within the range 12.10%-15.30%, while that of France is bounded by -0.3% and 0.3%. This seems to suggest that Belgium behaved more like the PIIGS countries than France does, as a result of the crisis.

The above empirical results show that accounting for country level (internal) risk factors may add some explanatory power to default rate models within the Euro area for ranking individual countries in terms of riskiness. However, rms are externally exposed to extra risk induced by the economic and nancial activities among the member states of the Euro area, and neglecting the potential impacts of group level (external) risk factors on rms' behaviour may likely lead to the underestimation of failure rates and related dependencies among rms. Further, rms listed within the periphery (weaker) group of countries experience higher risk level compared to those listed in the non-periphery (stronger) group in the Euro area.

# 4 Conclusion

The estimates of failure probability and its correlation play an important role in contemporary risk management for corporations, regulators, investors and academics (see Shumway, 2001; Du e et al., 2007; Duan et al., 2012, among others).

In this paper we employ a mixed e ects Cox model that accounts for nested unobserved factors to investigate the hazard rates and dependence structures of public listed rms of the stock exchanges in 11 Euro countries. The model embodies both country (internal) and group level (external) risk unobserved factors. For comparison purpose, we also consider a non-nested frailty model, which only incorporates unobserved factors at country level.

In the empirical analysis, we employ covariates largely used in the empirical literature, such as distance to default probability, one year trailing stock return, one year trailing market return, rm age, and 3 month T-bill rate, and consider four di erent groups of countries for the nested frailty model, namely PIIGS, PIIGSBF (Belgium and France are included in the

paper examines the impact of rms' membership to groups of the Euro area on riskiness.

Further research may consider a three level nested frailty model that accounts for sector level exposures in addition to country and group levels. This is because rms may be subjected to some industry level regulatory requirements and competition which may in uence their risk levels.

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